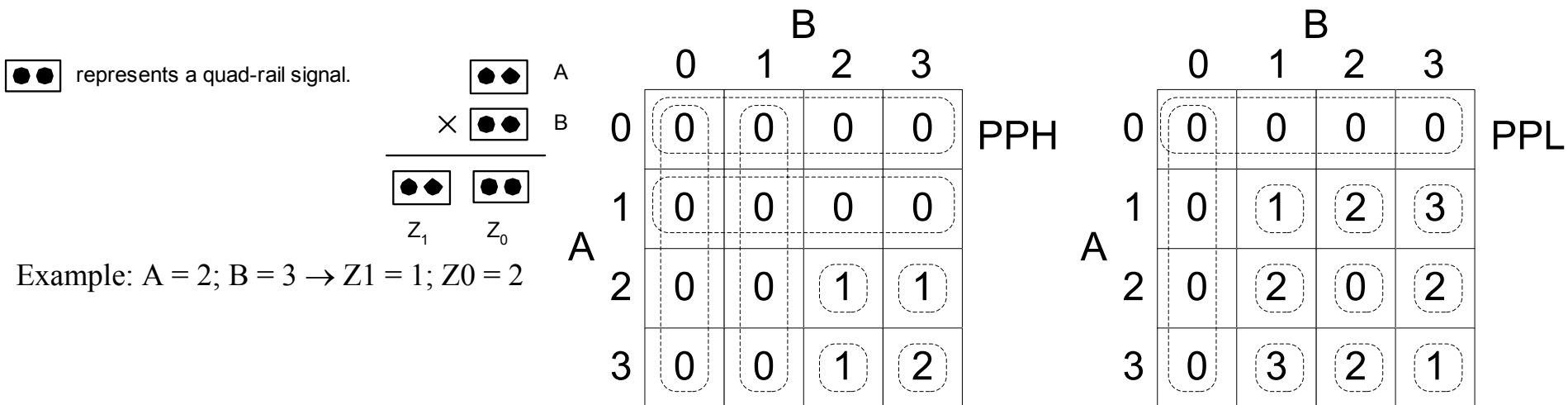


Quad-Rail Combinational Circuit Design

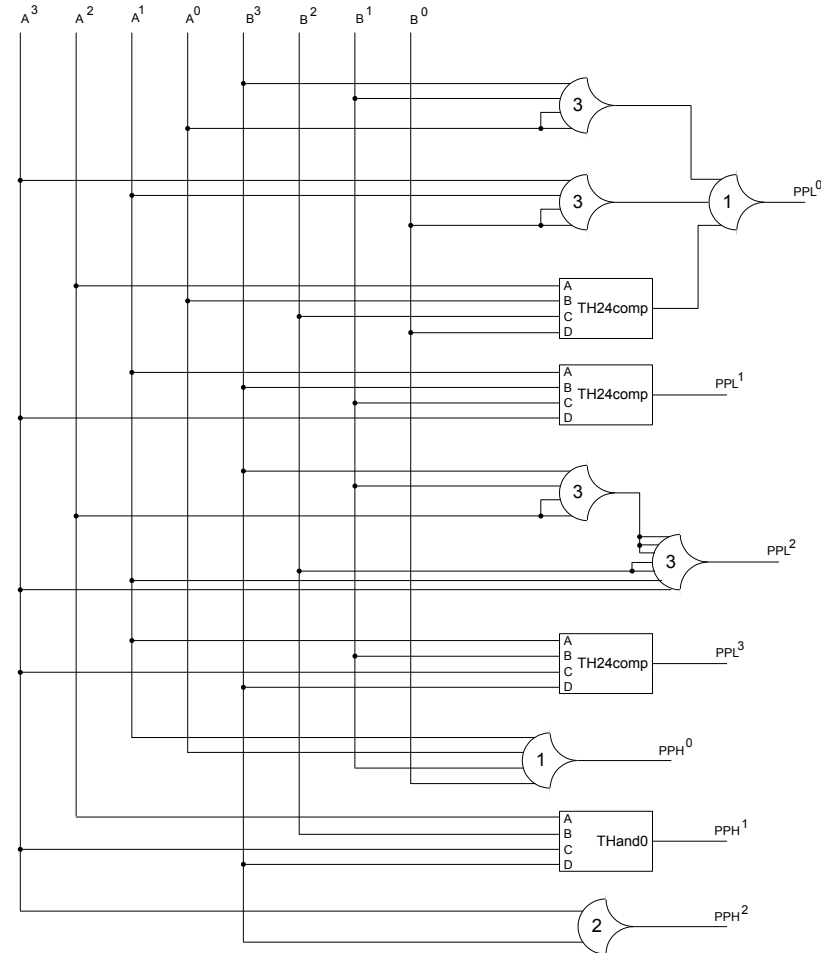
- $0s, 1s, 2s, 3s$ refer to a signal's $rail^0, rail^1, rail^2, rail^3$, respectively
- Add missing terms to ensure input-completeness
- Partition output equations into groups of four or fewer variables
 - largest number of product terms per group
 - smallest number of groups
 - map each group to one of the 27 NCL gates
- Only 4-coverings can be utilized to eliminate a quad-rail signal from the corresponding product term
- Input order does not need to be rearranged like required for Boolean and dual-rail K-maps

Quad-rail PP Generation Component

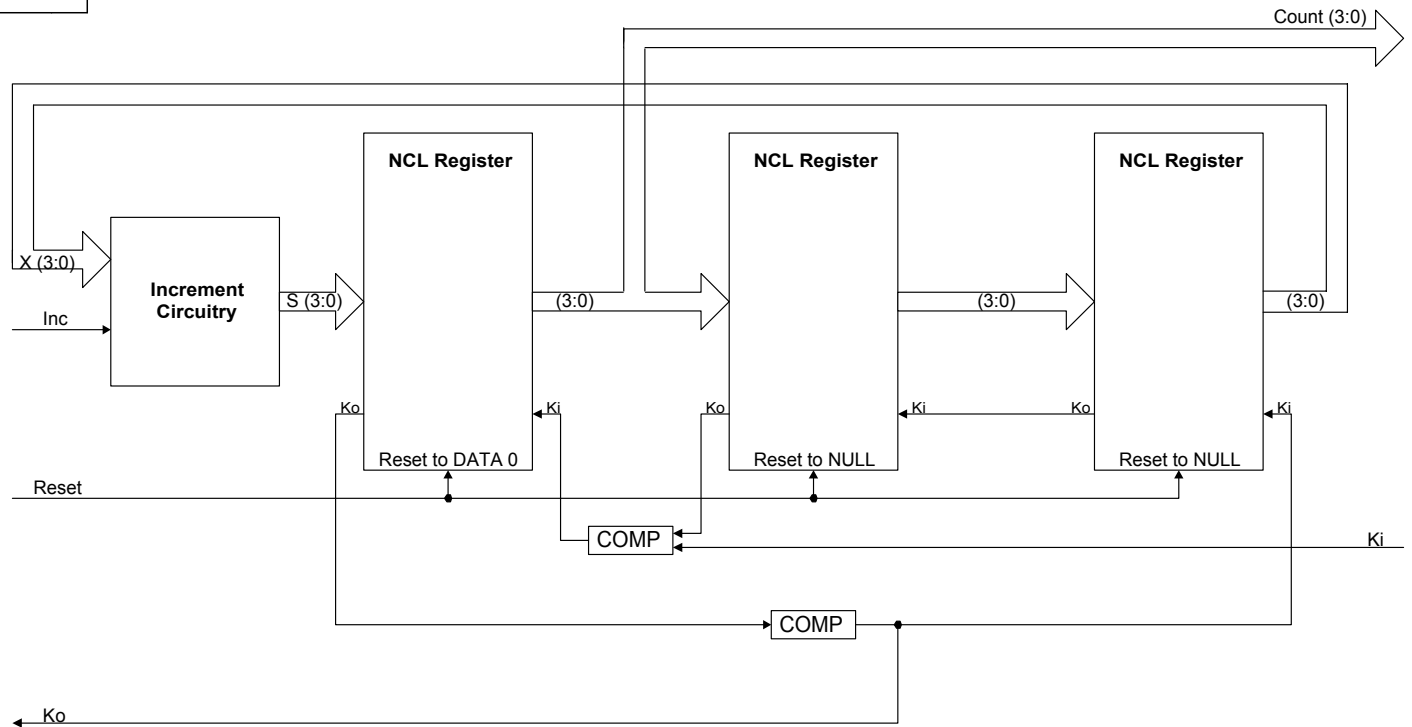
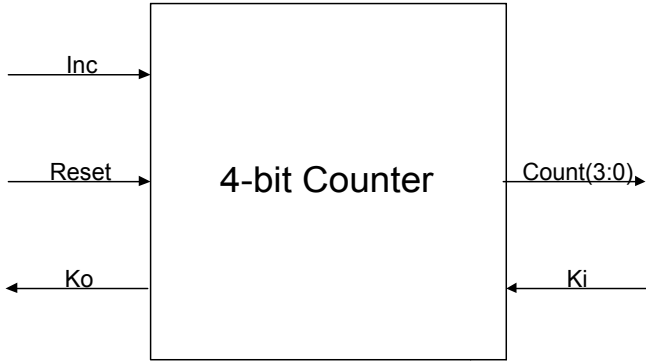


Optimized Quad-Rail PP Generation Component

- $PPL^0 = A^0 + B^0 + A^2B^2 = A^0 \bullet (B^0 + B^1 + B^2 + B^3) + B^0 \bullet (A^0 + A^1 + A^2 + A^3) + A^2B^2$
 $= A^0B^3 + A^0B^1 + A^3B^0 + A^1B^0 + A^2B^2 + A^2B^0 + A^0B^2 + A^0B^0$
- $PPL^1 = A^1B^1 + A^3B^3 = A^1B^1 + A^3B^3 + A^1A^3 + B^1B^3$
- $PPL^2 = A^2B^1 + A^2B^3 + A^1B^2 + A^3B^2$
- $PPL^3 = A^1B^3 + A^3B^1 = A^1B^3 + A^3B^1 + A^1A^3 + B^1B^3$
- $PPH^0 = A^0 + A^1 + B^0 + B^1$
- $PPH^1 = A^2B^2 + A^2B^3 + A^3B^2$
- $PPH^2 = A^3B^3$

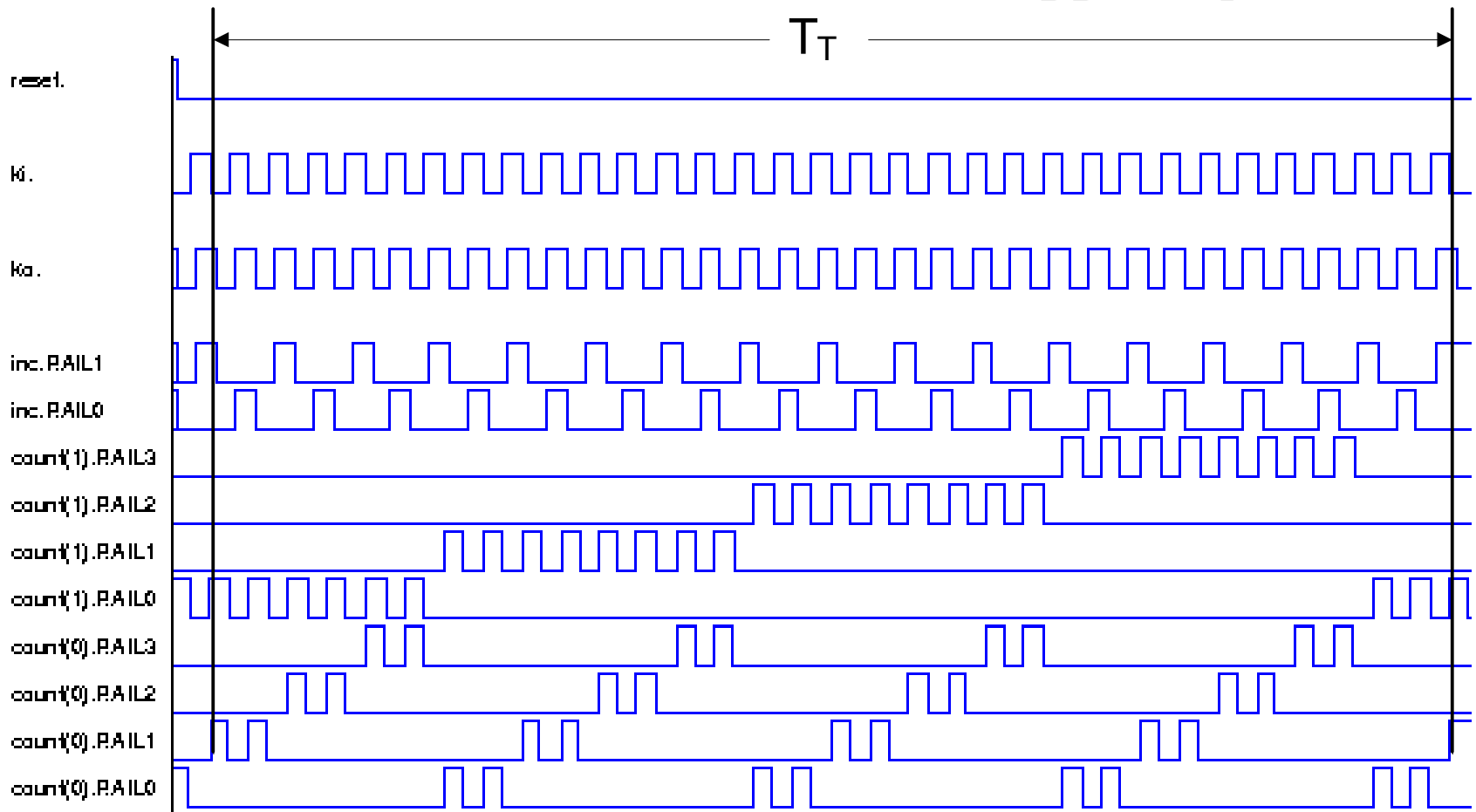


Counter Overview



Quad-Rail Counter Waveforms

- There are 32 possible combinations of the 5 circuit inputs (i.e. $2^5 = 32$)
- Average DATA-to-DATA cycle time: $T_{DD} = T_T / 32$



Quad-Rail Increment Circuitry K-Maps

		X_0			
		0	1	2	3
Inc	0	0	1	2	3
	1	1	2	3	0

S_0

		Inc = 0			
		X_0			
		0	1	2	3
X_1	0	0	0	0	0
	1	1	1	1	1
	2	2	2	2	2
	3	3	3	3	3

		Inc = 1			
		X_0			
		0	1	2	3
X_1	0	0	0	0	1
	1	1	1	1	2
	2	2	2	2	3
	3	3	3	3	0

S_1

- $S_0^0 = \text{Inc}^0 X_0^0 + \text{Inc}^1 X_0^3$
- $S_0^1 = \text{Inc}^0 X_0^1 + \text{Inc}^1 X_0^0$
- $S_0^2 = \text{Inc}^0 X_0^2 + \text{Inc}^1 X_0^1$
- $S_0^3 = \text{Inc}^0 X_0^3 + \text{Inc}^1 X_0^2$
- $S_1^0 = \text{Inc}^0 X_1^0 + X_0^0 X_1^0 + X_0^1 X_1^0 + X_0^2 X_1^0 + \text{Inc}^1 X_0^3 X_1^3$
- $S_1^1 = \text{Inc}^0 X_1^1 + X_0^0 X_1^1 + X_0^1 X_1^1 + X_0^2 X_1^1 + \text{Inc}^1 X_0^3 X_1^0$
- $S_1^2 = \text{Inc}^0 X_1^2 + X_0^0 X_1^2 + X_0^1 X_1^2 + X_0^2 X_1^2 + \text{Inc}^1 X_0^3 X_1^1$
- $S_1^3 = \text{Inc}^0 X_1^3 + X_0^0 X_1^3 + X_0^1 X_1^3 + X_0^2 X_1^3 + \text{Inc}^1 X_0^3 X_1^2$

Optimized Quad-Rail Increment Circuitry

$$S_1^0 = X_1^0 \bullet (\text{Inc}^0 + X_0^0 + X_0^1 + X_0^2) + X_1^3 \bullet (\text{Inc}^1 X_0^3) + (\text{Inc}^0 + X_0^0 + X_0^1 + X_0^2) \bullet (\text{Inc}_1 X_0^3) + X_1^0 X_1^3$$

$$S_1^1 = X_1^1 \bullet (\text{Inc}^0 + X_0^0 + X_0^1 + X_0^2) + X_1^0 \bullet (\text{Inc}^1 X_0^3) + (\text{Inc}^0 + X_0^0 + X_0^1 + X_0^2) \bullet (\text{Inc}_1 X_0^3) + X_1^0 X_1^1$$

$$S_1^2 = X_1^2 \bullet (\text{Inc}^0 + X_0^0 + X_0^1 + X_0^2) + X_1^1 \bullet (\text{Inc}^1 X_0^3) + (\text{Inc}^0 + X_0^0 + X_0^1 + X_0^2) \bullet (\text{Inc}_1 X_0^3) + X_1^1 X_1^2$$

$$S_1^3 = X_1^3 \bullet (\text{Inc}^0 + X_0^0 + X_0^1 + X_0^2) + X_1^2 \bullet (\text{Inc}^1 X_0^3) + (\text{Inc}^0 + X_0^0 + X_0^1 + X_0^2) \bullet (\text{Inc}_1 X_0^3) + X_1^2 X_1^3$$

$$S_0^0 = \text{Inc}^0 X_0^0 + \text{Inc}^1 X_0^3 + \text{Inc}^0 \text{Inc}^1 + X_0^0 X_0^3$$

$$S_0^1 = \text{Inc}^0 X_0^1 + \text{Inc}^1 X_0^0 + \text{Inc}^0 \text{Inc}^1 + X_0^0 X_0^1$$

$$S_0^2 = \text{Inc}^0 X_0^2 + \text{Inc}^1 X_0^1 + \text{Inc}^0 \text{Inc}^1 + X_0^1 X_0^2$$

$$S_0^3 = \text{Inc}^0 X_0^3 + \text{Inc}^1 X_0^2 + \text{Inc}^0 \text{Inc}^1 + X_0^2 X_0^3$$

